



Practical Tools for Measurement Systems Analysis

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Practical Tools for Measurement Systems Analysis

Presentation Outline

- Conventional Gage R&R Metrics – basic familiarity assumed
- Thought process for Measurement Systems Analysis
- Practical approaches and tools
- Examples

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- Measurement Systems Analysis – Gage R&R
 - Assesses Repeatability and Reproducibility
- Metric-based way of drawing conclusions from Gage R&R Studies: percentages per AIAG MSA Handbook
 - %Study Variation: compares measurement system variation to overall variation (measurement system and part-to-part)
 - %Tolerance: compares measurement system variation to tolerance
 - Guidelines: 10/30% rule

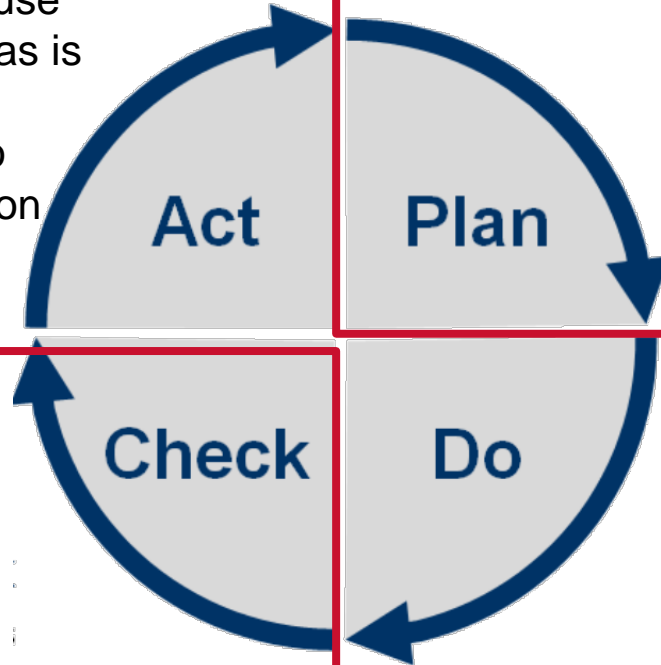
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Measurement Systems Analysis Process

Decision

1. Results satisfactory – use measurement system as is
2. Collect more data
3. Make improvements to current system based on findings

- Study results
- Assess if results are in line with expectations



- Define scope
- Measurement application
- Sample selection strategy
- Strategy for appraisers
- Define execution plan
- Data collection plan
- Assessment criteria

- Execute study based on plan

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- **“PGA” Approach**
 - Practical
 - Graphical
 - Analytical

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Practical

- Going into the study: what is the purpose of the measurement?
 - How big of a difference am I trying to detect? “Signal to Noise”
 - What are my specification limits? Where is my process running?
- Is there anything about the raw data that visually stands out?

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Graphical

- Graphical look
- Is there anything about the data that graphically stands out?
- Chart study results and look for clues – shifts, drifts, patterns, special causes etc.

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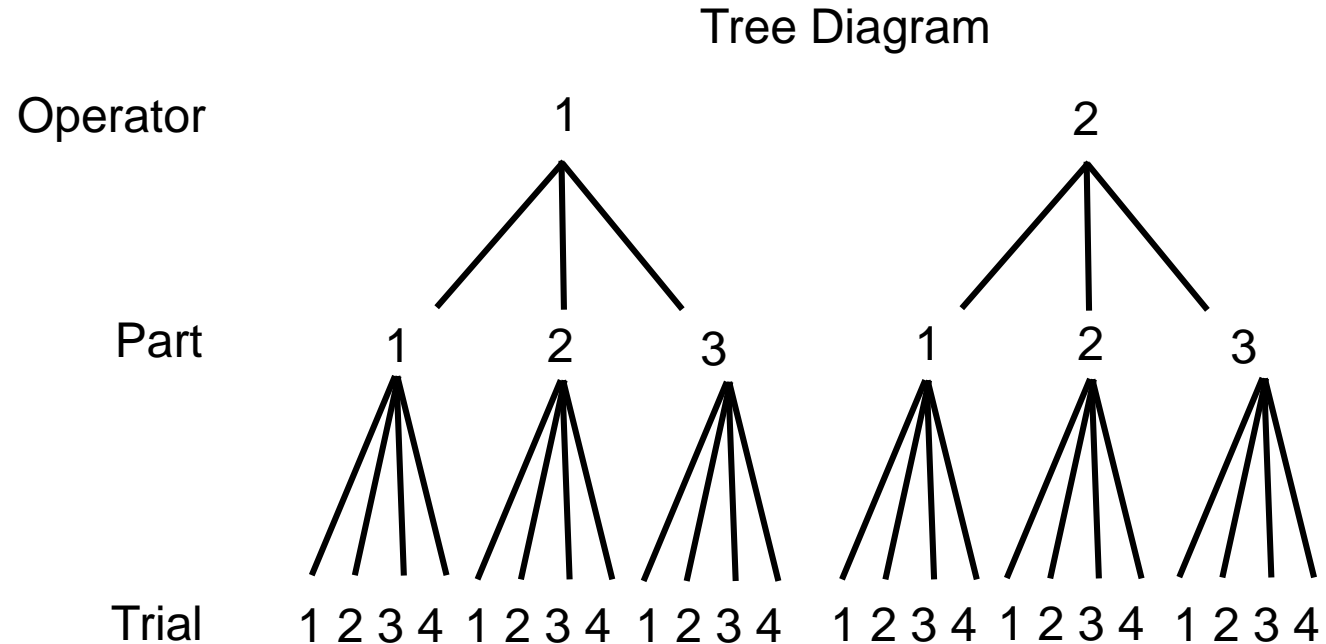
Analytical

- This should be the last step of your analysis
- Be careful about what you choose to be the metric of the analysis

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Example of PGA Approach: Gage R&R for optical wall thickness measurement

- Optical measurement
- Extruded components
- Specification: .012"-.013"



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Practical

Visual – Raw data

Specification: .012”-.013”

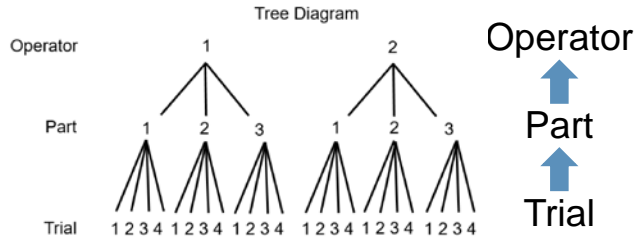
| Sample | Operator | Trial | WT |
|--------|----------|-------|---------|
| 1 | 1 | 1 | 0.01205 |
| 2 | 1 | 1 | 0.01247 |
| 3 | 1 | 1 | 0.01200 |
| 1 | 1 | 2 | 0.01206 |
| 2 | 1 | 2 | 0.01248 |
| 3 | 1 | 2 | 0.01196 |
| 1 | 1 | 3 | 0.01206 |
| 2 | 1 | 3 | 0.01247 |
| 3 | 1 | 3 | 0.01197 |
| 1 | 1 | 4 | 0.01206 |
| 2 | 1 | 4 | 0.01247 |
| 3 | 1 | 4 | 0.01203 |
| 1 | 2 | 1 | 0.01203 |
| 2 | 2 | 1 | 0.01250 |
| 3 | 2 | 1 | 0.01195 |
| 1 | 2 | 2 | 0.01199 |
| 2 | 2 | 2 | 0.01251 |
| 3 | 2 | 2 | 0.01188 |
| 1 | 2 | 3 | 0.01197 |
| 2 | 2 | 3 | 0.01250 |
| 3 | 2 | 3 | 0.01198 |
| 1 | 2 | 4 | 0.01201 |
| 2 | 2 | 4 | 0.01242 |
| 3 | 2 | 4 | 0.01189 |

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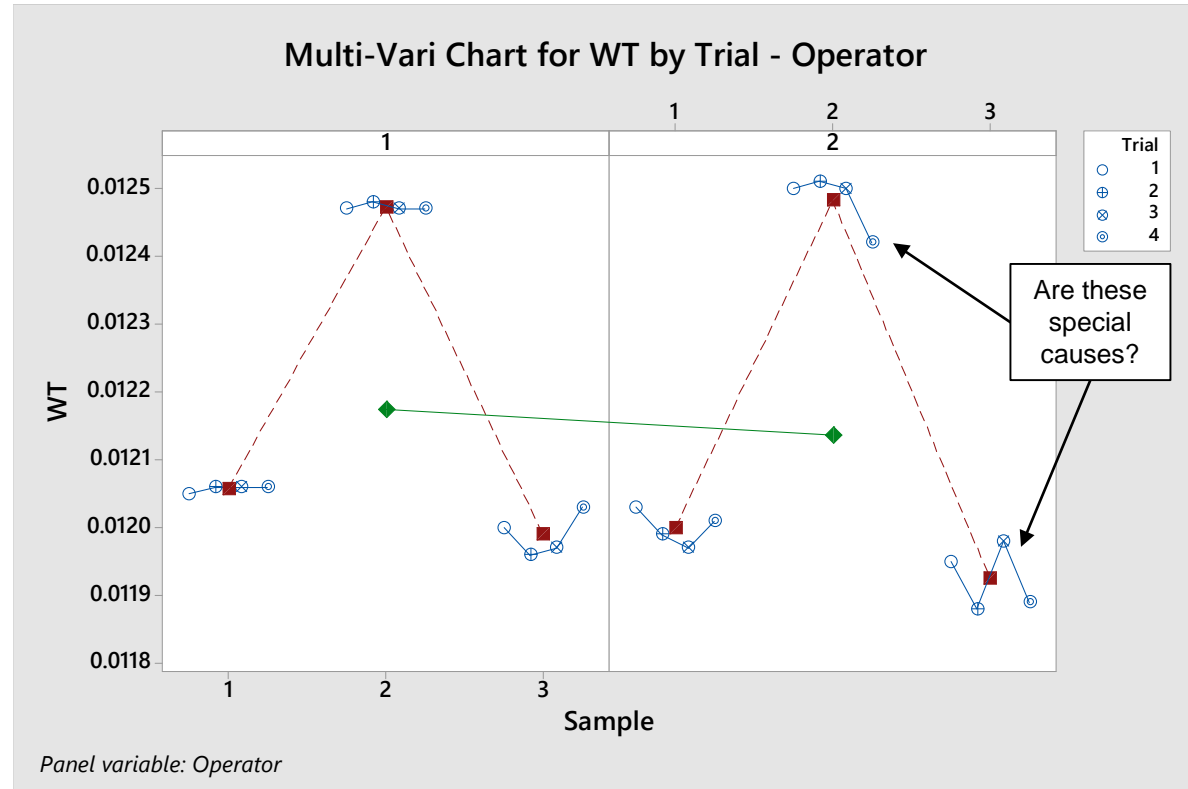
Graphical

Tool: Multi-Vari Chart

- Ability to compare variation across factors
- Bottom-up



- Ability to look for patterns in the data



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Graphical & Analytical I.

Tool: Xbar-R behavior chart

- Charts staged by operator

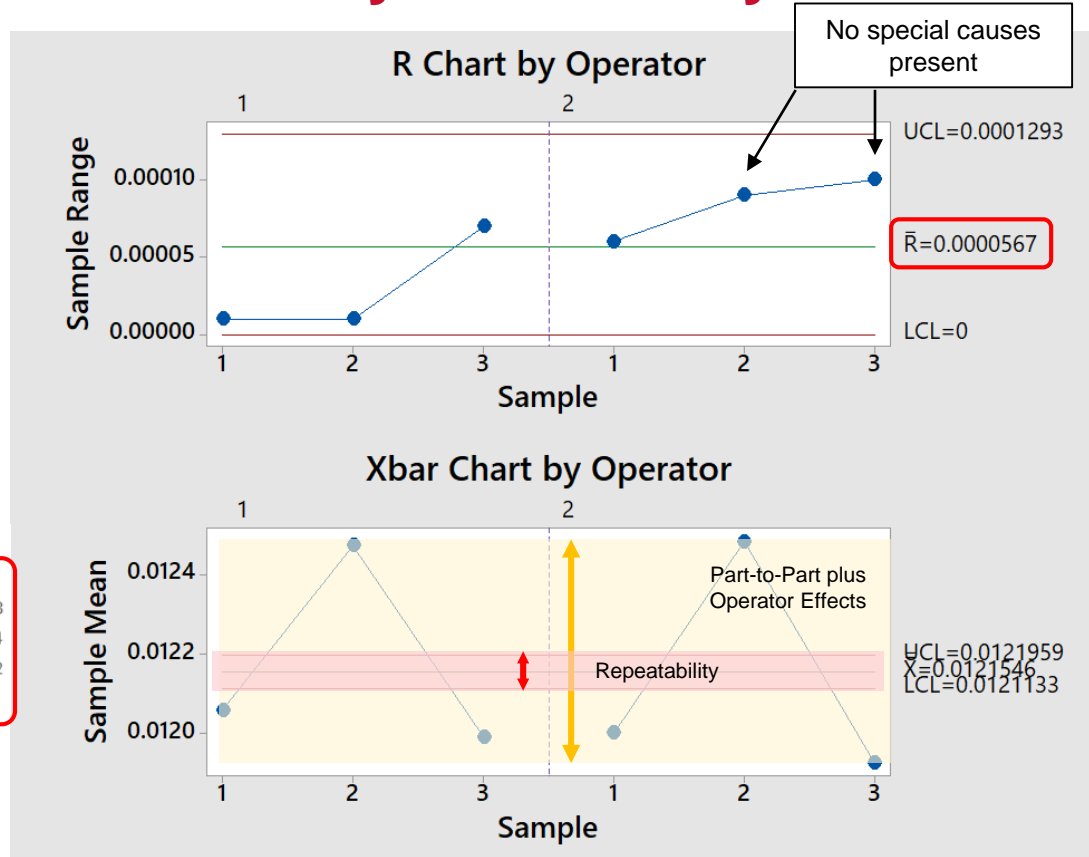
$$UCL_R = D_4 * \bar{R} \quad UCL_x = \bar{\bar{X}} + A_2 * \bar{R}$$

$$LCL_R = D_3 * \bar{R} \quad LCL_x = \bar{\bar{X}} - A_2 * \bar{R}$$

Tabular values for X-bar and range charts

| Subgroup Size | A ₂ | d ₂ | D ₃ | D ₄ |
|---------------|----------------|----------------|----------------|----------------|
| 2 | 1.880 | 1.128 | ---- | 3.268 |
| 3 | 1.023 | 1.693 | ---- | 2.574 |
| 4 | 0.729 | 2.059 | ---- | 2.282 |
| 5 | 0.577 | 2.326 | ---- | 2.114 |

- Xbar chart shows repeatability vs. part-to-part variation



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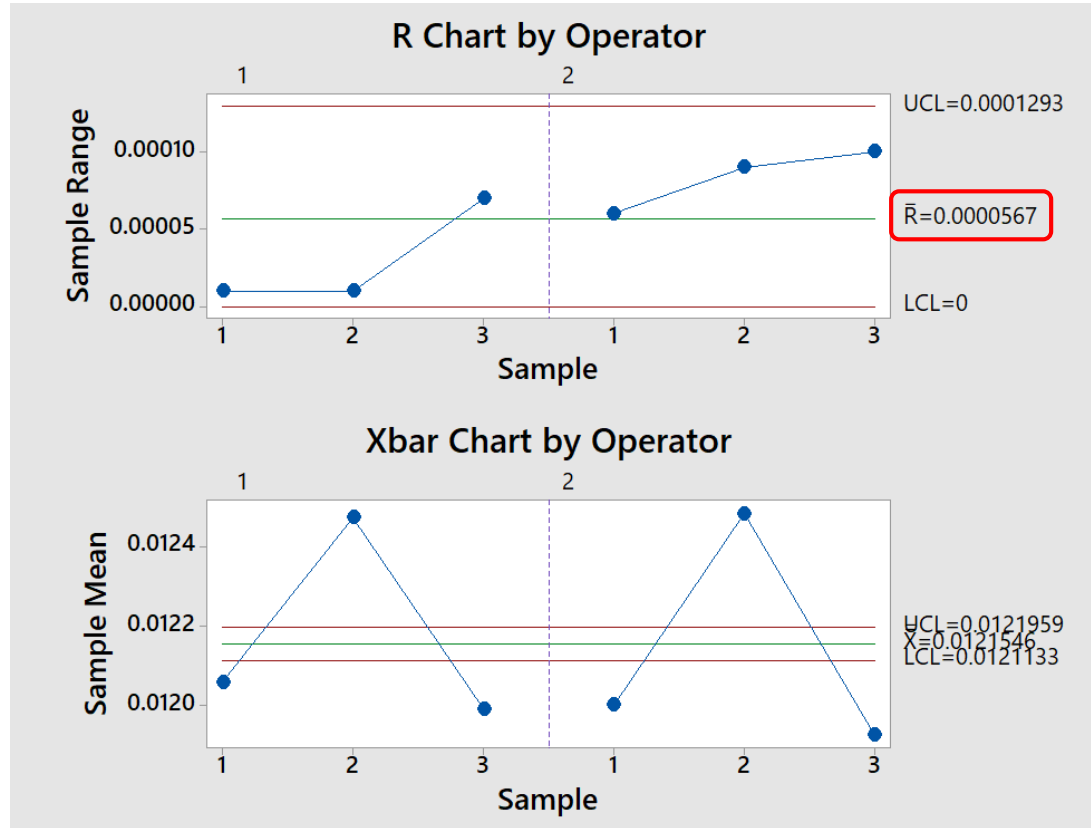
Graphical & Analytical II.

Tool: Xbar-R behavior chart

- Rbar: represents average repeatability error
- Ranges above control limit on R chart need to be investigated



Graphical – Multi-Vari Chart



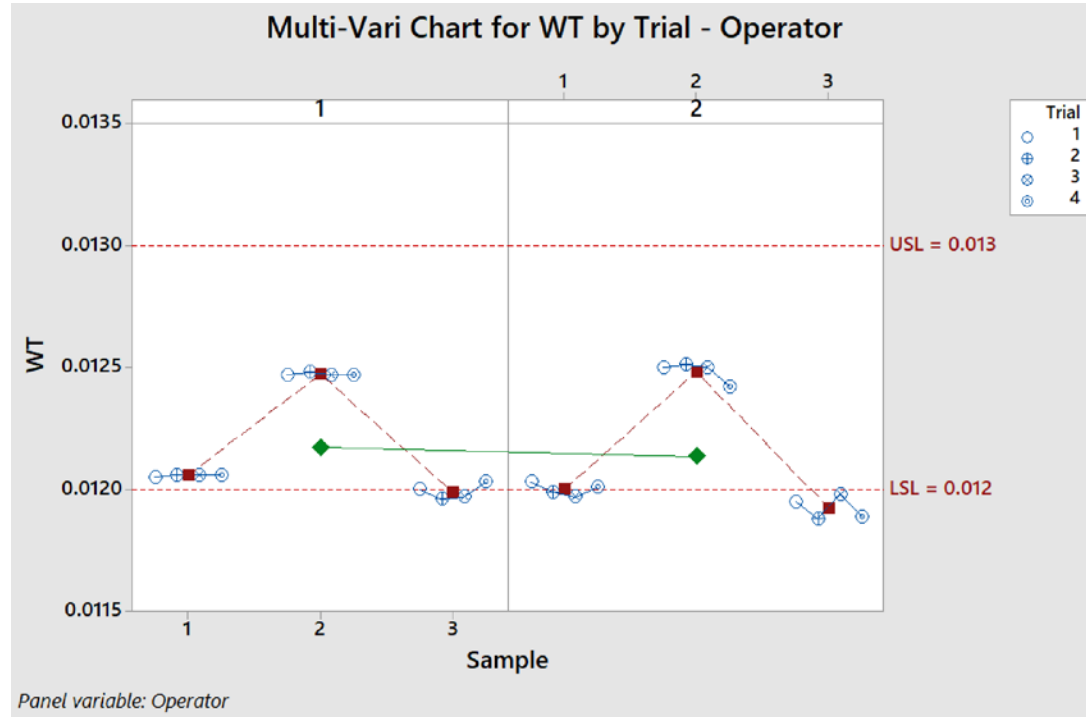
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Making a Decision

Scenario #1

Process running close to LSL causing yield issues. Engineer identifies critical process parameters and decides to run a DOE to bring process to nominal

- How big of a difference do you want to be able to detect?
- $R_{bar} = 0.0000567''$
- Is the measurement system acceptable for this scenario?



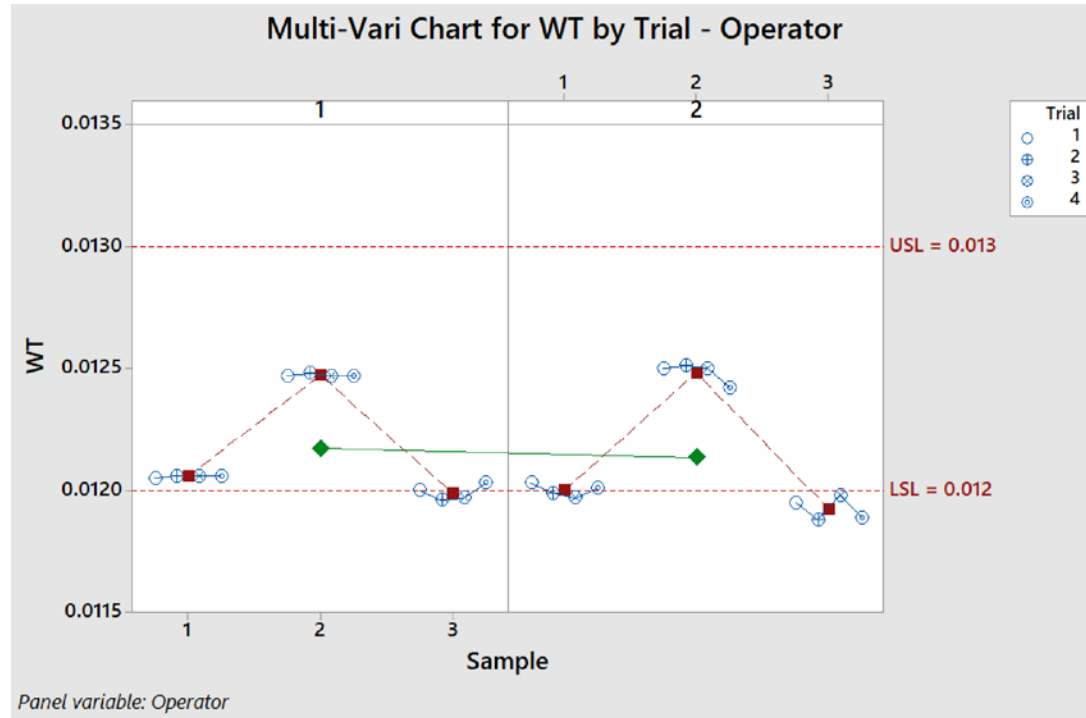
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Making a Decision

Scenario #2

Process running close to LSL causing yield issues. Engineer decides to perform 100% sorting

- What is the purpose of the inspection?
- $R_{\text{bar}} = 0.0000567''$
- %Tolerance = 25.53%Tol.
 - Repeatability = 20.85%Tol.
 - Reproducibility = 14.73%Tol.
- Is the measurement system acceptable for this scenario?
- What is the risk the engineer is running?



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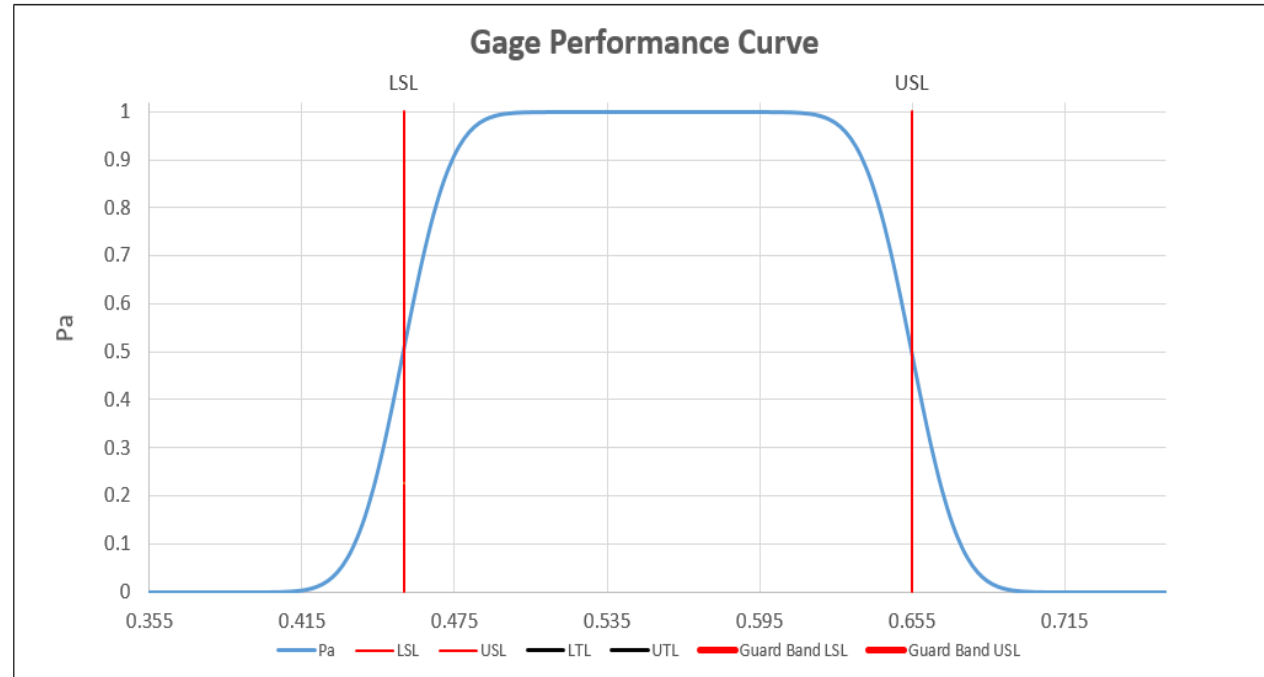
Risk-Based Approach

- Risk of product misclassification
 - Good \longrightarrow Bad
 - Bad \longrightarrow Good
- The closer you are to the specification limits, the higher the risk of misclassification
- How does one quantify the risk of misclassification?

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Gage Performance Curve

- Visualizes and quantifies risk of misclassification
- Plotted for individual reference values covering the entire tolerance range and outside of it
- Uses Gage R&R results (StDev) and Z score-based probability calculations to quantify risk



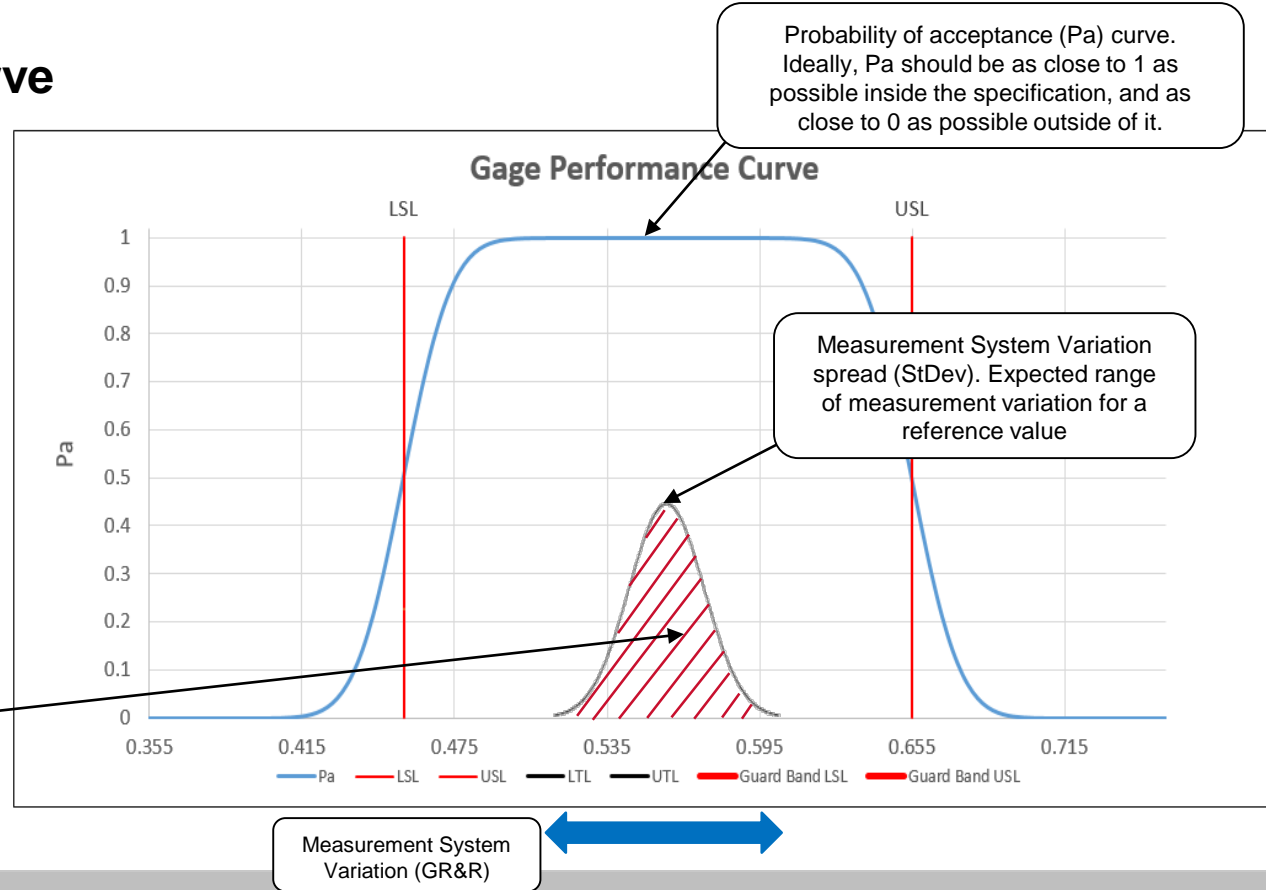
Formula:
$$P_a = \phi\left(\frac{UL - (X_T + b)}{\sigma}\right) - \phi\left(\frac{LL - (X_T + b)}{\sigma}\right)$$

Source: AIAG MSA Reference Manual, 4th Edition

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Gage Performance Curve

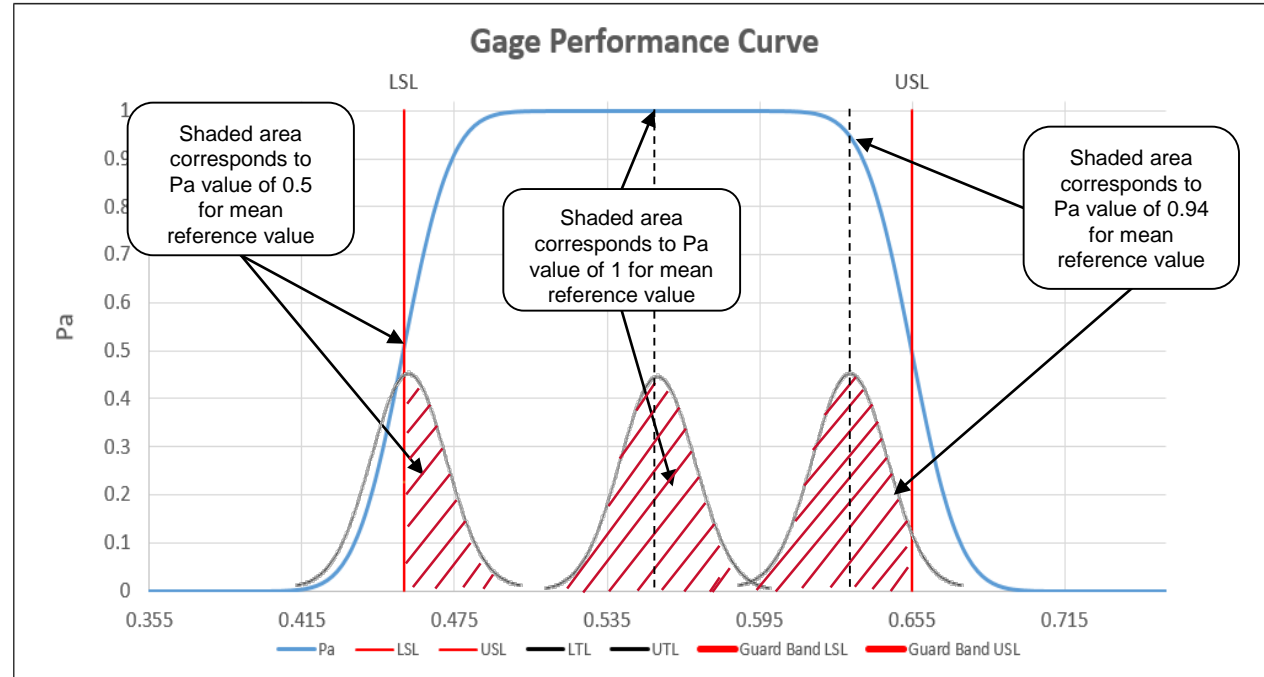
| Measurement System Variation | |
|------------------------------|----------|
| LSL | 0.455 |
| USL | 0.655 |
| Sigma Interval | 5.62 |
| StdevGRR | 0.015 |
| Variance | 0.000225 |
| %Tolerance | 42.15% |



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Gage Performance Curve

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How do you address the risk of misclassification?

→ through Guard Banding

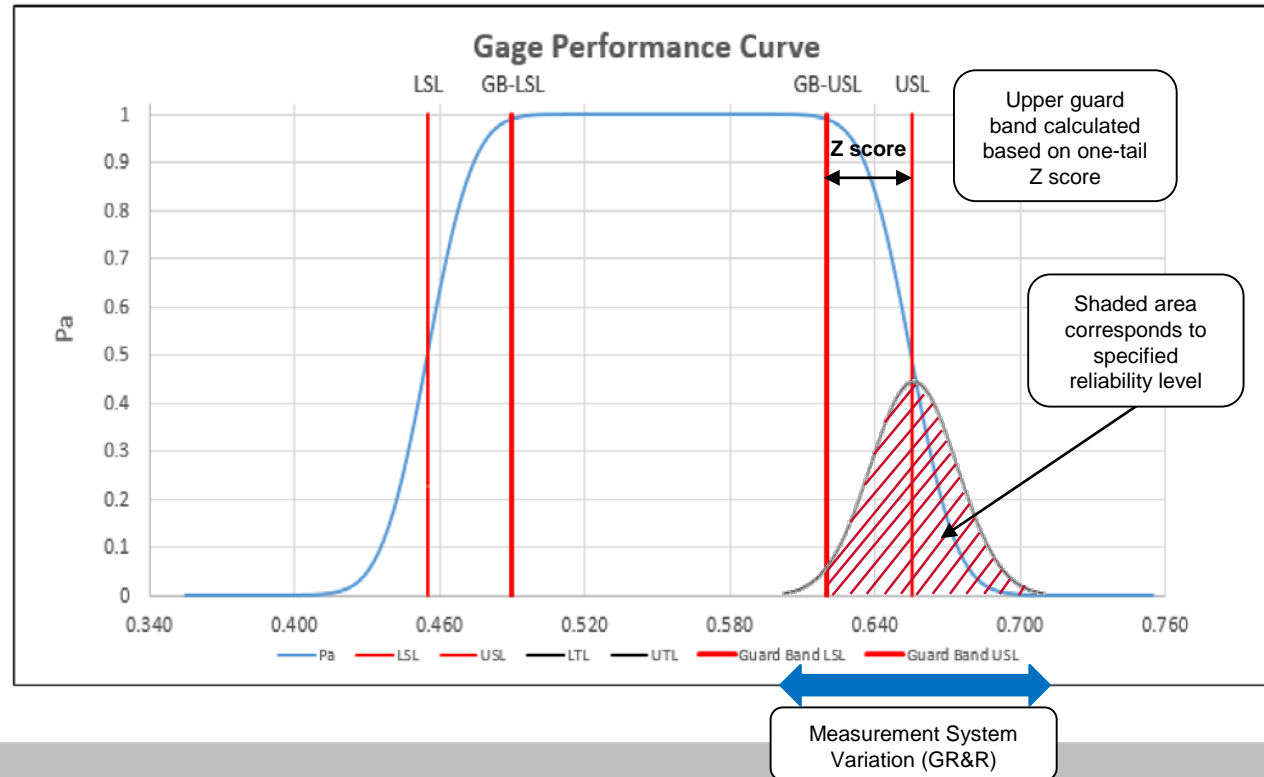
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Guard Banding

- Guard band applied around specification limits
- Guard band width a fraction of measurement system variation

Guard Banding Excel Tool – email me at gabor.attila.szabo@gmail.com to get a copy

| Guard Banding | |
|------------------|---------|
| Guard Banding | Yes |
| Reliability | 99% |
| Guard banded LSL | 0.48995 |
| Guard banded USL | 0.62005 |

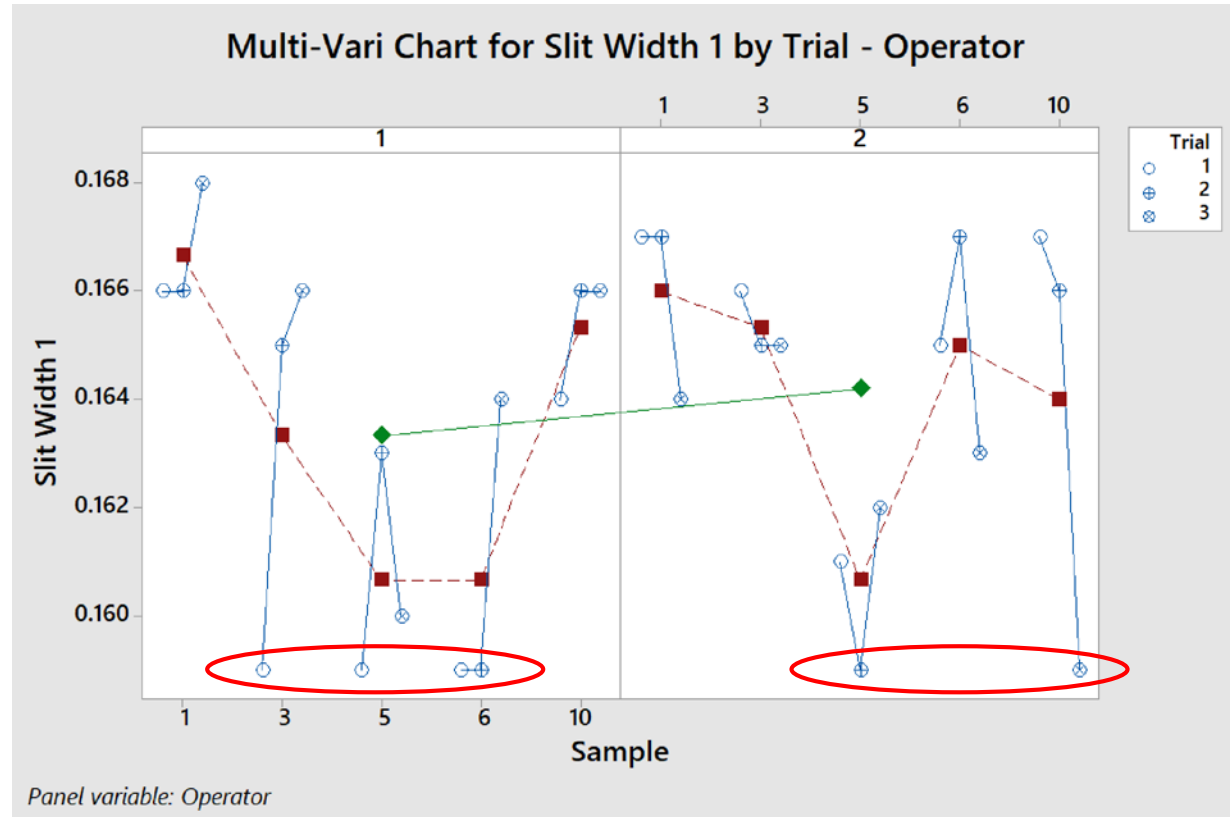


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Examples

#1

Is there anything about the charted data that stands out?



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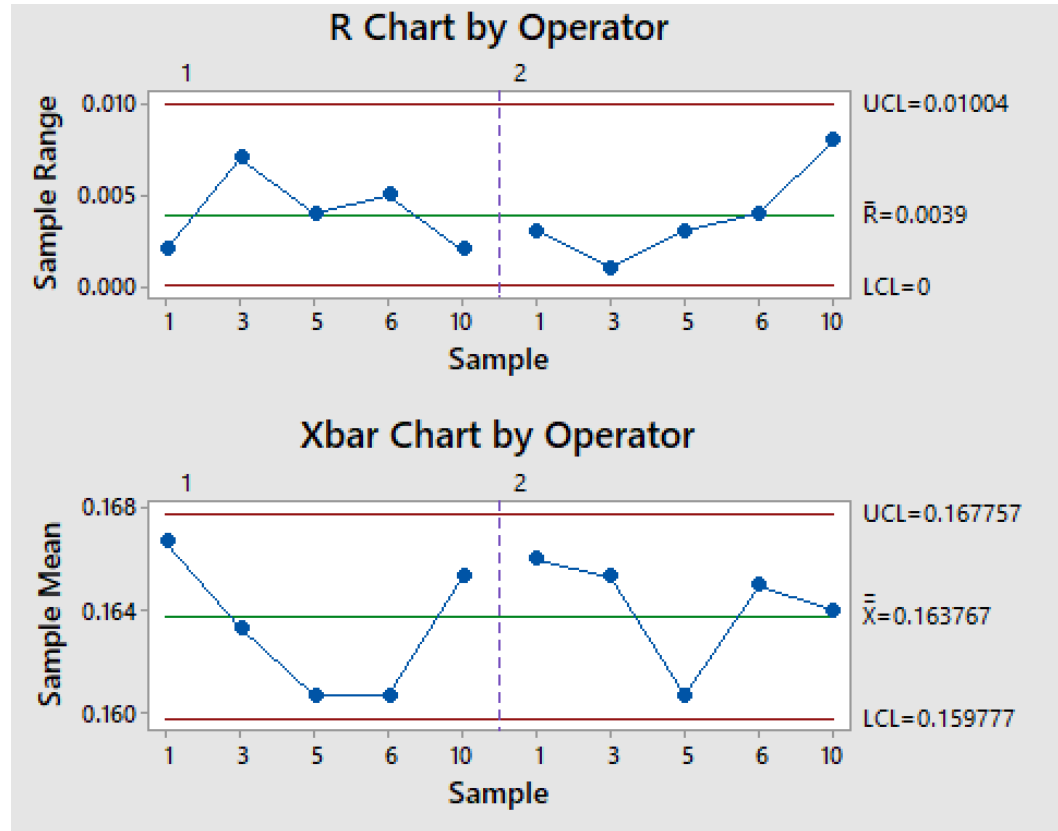
Examples

#1

- R chart: none of the ranges appear to be above the UCL
- Repeatability error exceeds part-to-part variation

Next steps:

- Investigate and eliminate special causes
- Assess whether further reduction of repeatability error is necessary

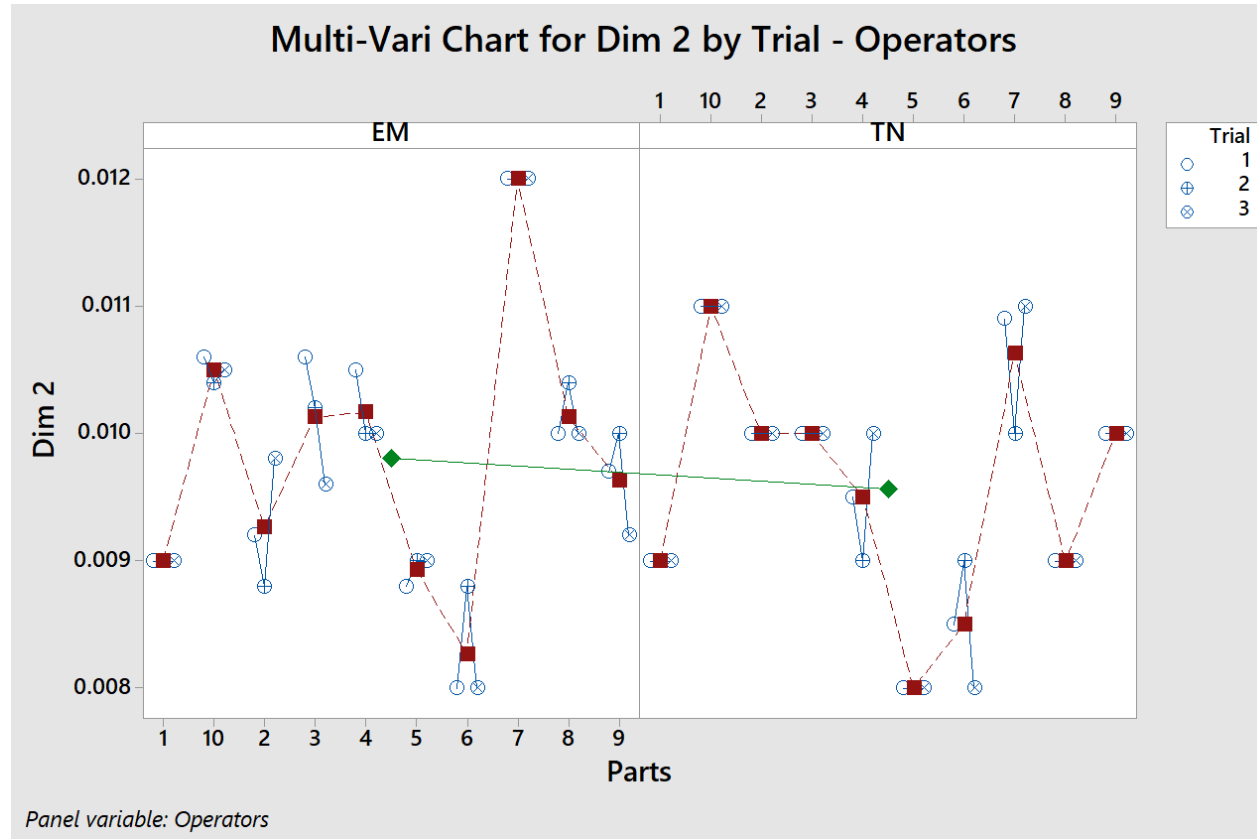


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Examples

#2

Is there anything about the charted data that stands out?



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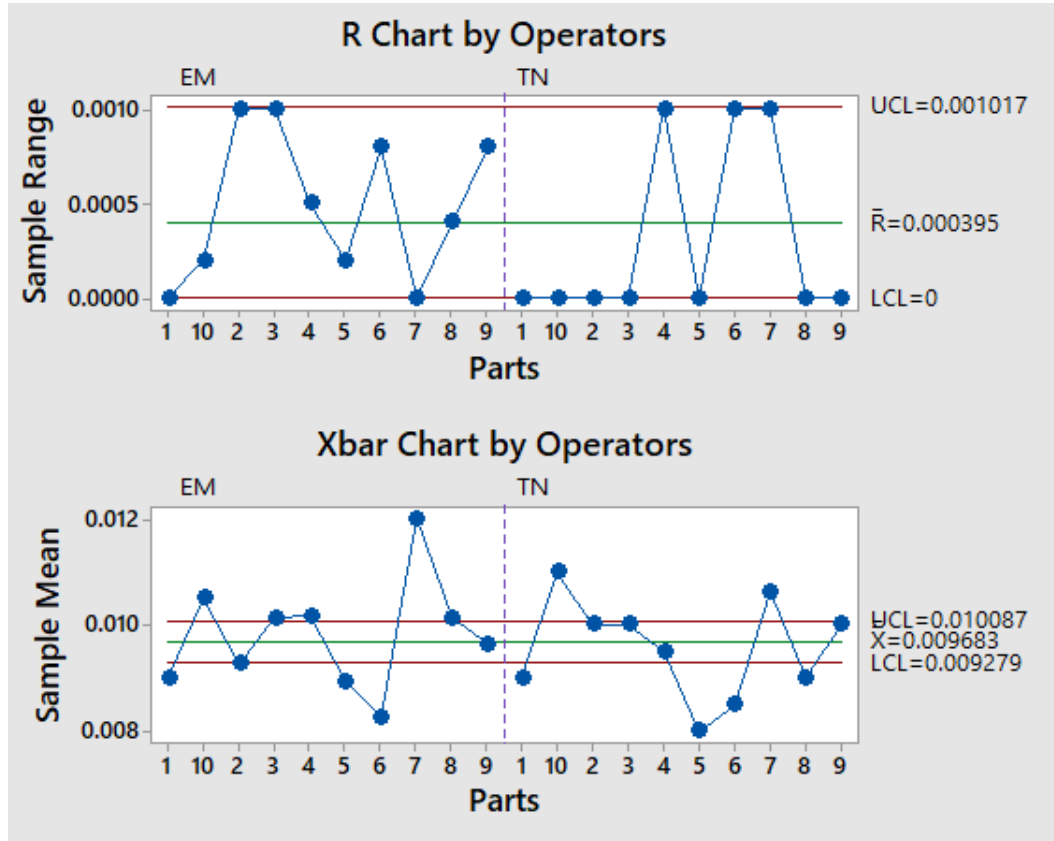
Examples

#2

- Resolution issue
- One of the operators (TN) rounded/truncated their measurement results

Next steps:

- Re-do study without rounding measurements
- Re-evaluate results



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Examples

#3

Is there anything about the raw data that stands out?

| Sample | Trial | Operator | Dimension |
|--------|-------|----------|-----------|
| 1 | 1 | 1 | 0.04121 |
| 1 | 2 | 1 | 0.04119 |
| 1 | 3 | 1 | 0.04115 |
| 1 | 4 | 1 | 0.04112 |
| 2 | 1 | 1 | 0.04138 |
| 2 | 2 | 1 | 0.04134 |
| 2 | 3 | 1 | 0.04128 |
| 2 | 4 | 1 | 0.04127 |
| 3 | 1 | 1 | 0.04114 |
| 3 | 2 | 1 | 0.04112 |
| 3 | 3 | 1 | 0.04109 |
| 3 | 4 | 1 | 0.04108 |
| 1 | 1 | 2 | 0.04120 |
| 1 | 2 | 2 | 0.04116 |
| 1 | 3 | 2 | 0.04114 |
| 1 | 4 | 2 | 0.04110 |
| 2 | 1 | 2 | 0.04113 |
| 2 | 2 | 2 | 0.04111 |
| 2 | 3 | 2 | 0.04102 |
| 2 | 4 | 2 | 0.04101 |
| 3 | 1 | 2 | 0.04138 |
| 3 | 2 | 2 | 0.04137 |
| 3 | 3 | 2 | 0.04135 |
| 3 | 4 | 2 | 0.04131 |

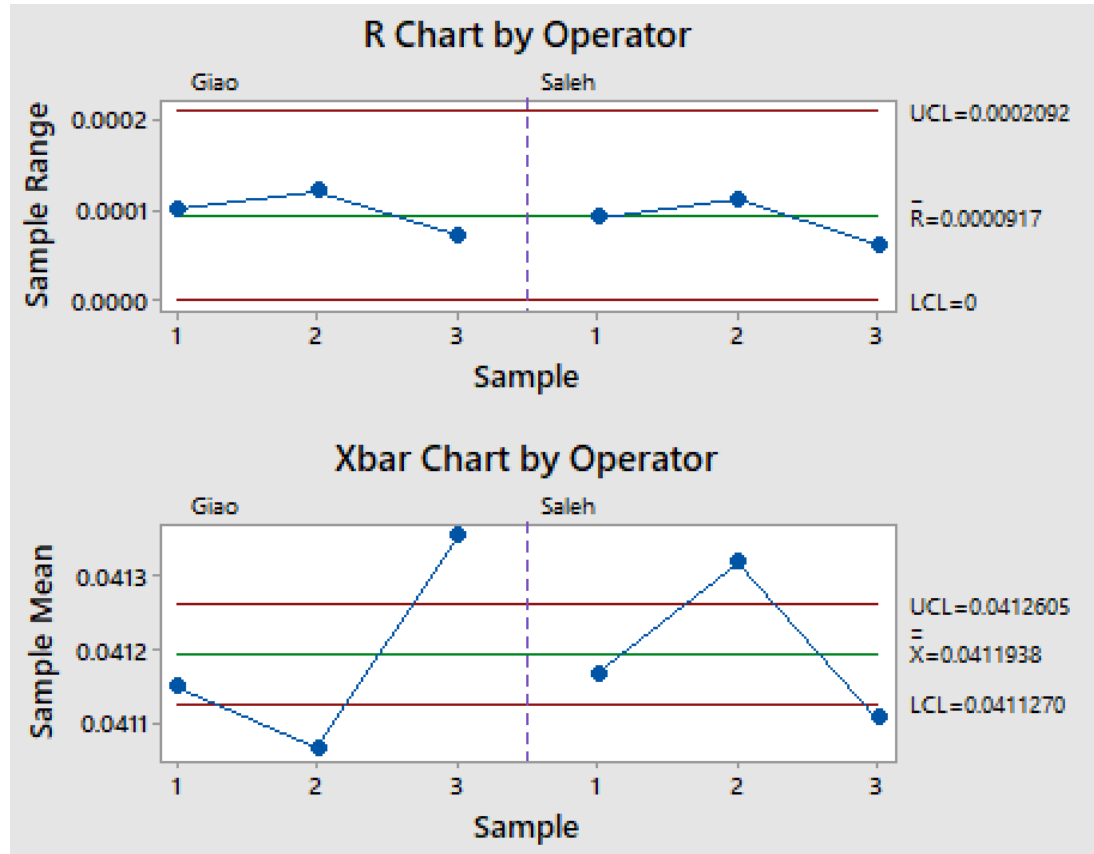
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Examples

#3

Is there anything about the charted data that stands out?

- R chart: none of the ranges appear to be above the UCL
- Repeatability error does not exceed part-to-part variation



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Examples

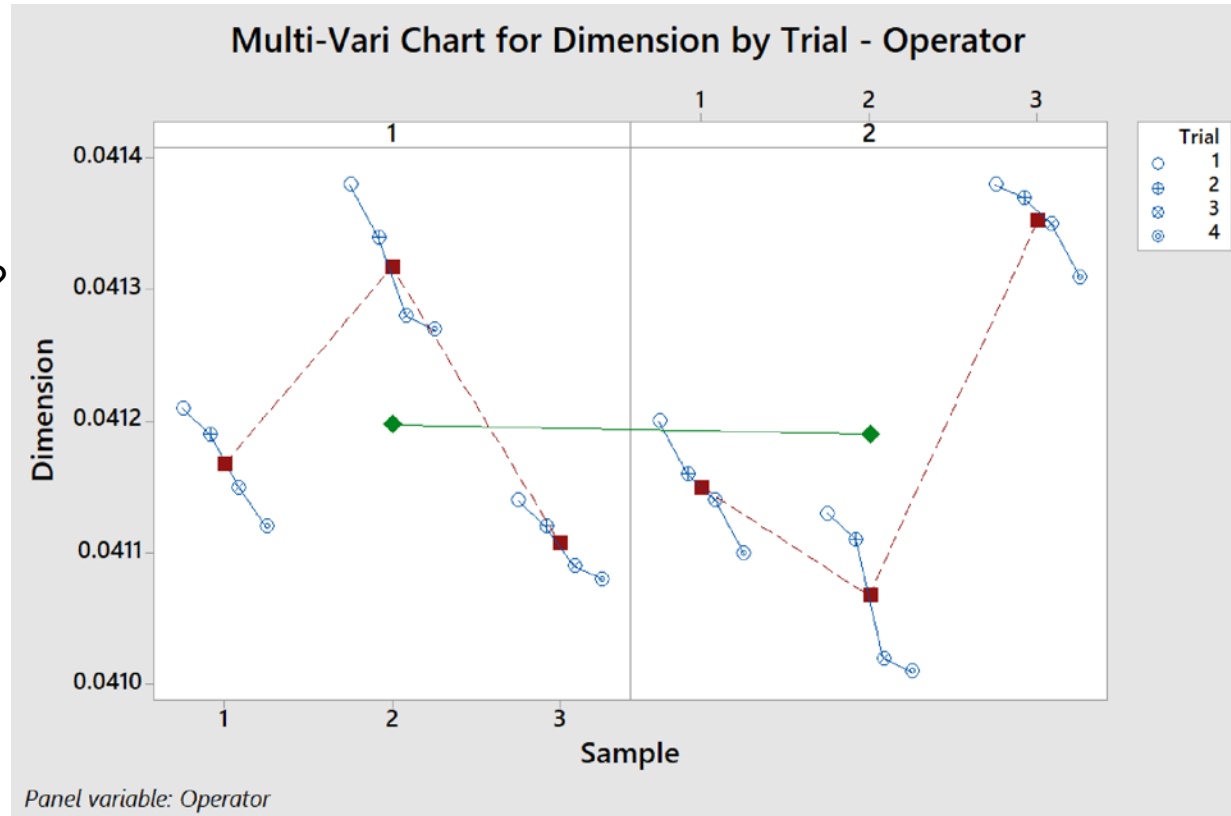
#3

Is there anything about the charted data that stands out?

- Decreasing pattern trial-to-trial

Next steps:

- Investigate the physics of the measurement or manufacturing process
- Investigate potential root causes



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Takeaways

- Don't rely solely on your conventional Gage R&R metrics to tell you how your measurement system is behaving
- Use the Practical-Graphical-Analytical (PGA) approach to study your measurement systems analysis result, look for patterns and take action based on findings
- Quantify risks associated with measurement error

Feel free to reach out with any questions!

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